

Package ‘wnpmle’

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Title Weighted NPMLE for Recurrent Events with a Competing Terminal Event

Version 0.1.3

Description Provides regression modeling and prediction for the marginal mean of recurrent events in the presence of a competing terminal event using the weighted nonparametric maximum likelihood estimator (wNPMLE) of Bellach and Kosorok (2026) [<doi:10.48550/arXiv.2605.25934>](https://doi.org/10.48550/arXiv.2605.25934). Two classes of transformation models are implemented: Box-Cox transformation models and logarithmic transformation models. These extend the proportional means model of Ghosh and Lin (2002) [<doi:10.17615/pt0g-y207>](https://doi.org/10.17615/pt0g-y207) and the transformation model framework of Zeng and Lin (2006) [<doi:10.1093/biomet/93.3.627>](https://doi.org/10.1093/biomet/93.3.627). Parameter estimation is performed using automatic differentiation through the Template Model Builder (TMB) framework. Standard errors are computed using sandwich variance estimators that account for estimation of the inverse-probability censoring weights following Bellach, Kosorok, Rüschemdorf and Fine (2019) [<doi:10.1080/01621459.2017.1401540>](https://doi.org/10.1080/01621459.2017.1401540).

License GPL (>= 3)

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URL <https://github.com/abellach/wnpmle>

BugReports <https://github.com/abellach/wnpmle/issues>

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AIC.wnpmle	<i>AIC for wnpmle objects</i>
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Description

AIC for wnpmle objects

Usage

```
## S3 method for class 'wnpmle'  
AIC(object, ..., k = 2)
```

Arguments

object	A wnpmle object.
...	Ignored.
k	Penalty per parameter (default 2 for AIC).

Value

A numeric scalar giving the AIC value.

baseline	<i>Extract the estimated baseline mean function</i>
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Description

Returns a data frame with the estimated cumulative baseline mean function $\Lambda(t)$ and its increments $\lambda(t)$, together with standard errors and pointwise 95% confidence intervals.

Usage

```
baseline(object, conf_level = 0.95, ...)
```

Arguments

object	A wnpml object.
conf_level	Confidence level for the pointwise intervals (default 0.95).
...	Ignored.

Value

A data frame with columns:

time	Recurrent event times.
lambda	Estimated baseline increments.
Lambda	Estimated cumulative baseline mean.
se_Lambda	Standard error of Lambda (if SE was estimated).
lower	Lower confidence band for Lambda.
upper	Upper confidence band for Lambda.

Examples

```
bdata <- bladder_prep()
bdata_clean <- bdata[, c("id", "time", "status", "treat", "num", "size")]
fit <- wnpml_fit(Surv(time, status) ~ treat + num + size,
                 data = bdata_clean, id = "id", model = "log", rho = 1)
bl <- baseline(fit)
head(bl)
```

BIC.wnrmle	<i>BIC for wnrmle objects</i>
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Description

BIC for wnrmle objects

Usage

```
## S3 method for class 'wnrmle'
BIC(object, ...)
```

Arguments

object	A wnrmle object.
...	Ignored.

Value

A numeric scalar giving the BIC value.

bladder_prep	<i>Prepare bladder cancer data for wnrmle analysis</i>
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Description

Prepares the bladder1 dataset from the **survival** package for use with [wnrmle_fit](#). Subjects randomised to pyridoxine are excluded (only placebo and thiotepa arms are retained). Status codes are recoded to 0 (censored), 1 (recurrent tumour), 2 (terminal/dropout), and event times beyond tau are truncated to tau.

Usage

```
bladder_prep(tau = 59)
```

Arguments

tau	Follow-up truncation time (default: 59 months). Event times beyond tau are set to tau.
-----	--

Details

The bladder cancer trial (Veterans Administration Cooperative Urological Research Group) randomised patients to placebo, pyridoxine, or thiotepa. Only the placebo and thiotepa arms are used here (pyridoxine arm excluded). Subjects with event times equal to tau and status 0 have their times truncated to tau, consistent with administrative censoring.

Value

A data frame with columns:

id	Subject identifier (integer).
status	Event status: 0 = censored, 1 = recurrent event, 2 = terminal event.
status0	Indicator: 1 if censored.
status1	Indicator: 1 if recurrent event.
status2	Indicator: 1 if terminal event.
time	Event time (months).
treat	Treatment indicator: 1 = thiotepa, 0 = placebo.
num	Initial number of tumours.
size	Initial tumour size (cm).

References

Byar, D.P. (1980). The Veterans Administration study of chemoprophylaxis for recurrent stage I bladder tumors. In *Bladder Tumors and Other Topics in Urological Oncology*, 363-370. Plenum, New York.

Examples

```
bdata <- bladder_prep(tau = 59)
head(bdata)
table(bdata$status)
```

coef.wnpmle

Extract coefficients from a wnpmle object

Description

Extract coefficients from a wnpmle object

Usage

```
## S3 method for class 'wnpmle'
coef(object, ...)
```

Arguments

object	A wnpmle object.
...	Ignored.

Value

A named numeric vector of regression coefficients.

logLik.wnpmle	<i>Log-likelihood for wnpmle objects</i>
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Description

Log-likelihood for wnpmle objects

Usage

```
## S3 method for class 'wnpmle'
logLik(object, ...)
```

Arguments

object	A wnpmle object.
...	Ignored.

Value

An object of class "logLik" with the log-likelihood value, degrees of freedom (df) equal to the number of regression coefficients, and number of observations (nobs).

plot.wnpmle	<i>Plot method for wnpmle objects</i>
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Description

Plots the estimated cumulative baseline mean function $\Lambda(t)$ with optional pointwise confidence bands.

Usage

```
## S3 method for class 'wnpmle'
plot(x, conf_bands = TRUE, ...)
```

Arguments

x	A wnpmle object.
conf_bands	Logical; if TRUE (default), adds pointwise 95% confidence bands when available.
...	Additional graphical parameters passed to plot.

Value

No return value, called for side effects (produces a plot).

plot_loglik

*Log-likelihood profile plot for the transformation parameter***Description**

Fits the model over a fine grid of transformation parameter values and plots the profile log-likelihood for both the Box-Cox and logarithmic transformation models on a single plot. The log transformation parameter r is shown on the left (negative axis) and the Box-Cox parameter ρ on the right (positive axis), meeting at zero where both models coincide.

Usage

```
plot_loglik(
  formula,
  data,
  id = "id",
  rho_grid = seq(0.01, 1.2, by = 0.01),
  r_grid = seq(0.01, 1.2, by = 0.01),
  tau = NULL,
  mark_points = TRUE,
  file = NULL,
  width = 6,
  height = 4.5,
  verbose = TRUE,
  ...
)
```

Arguments

formula	A formula as passed to wnpml_fit .
data	A data frame.
id	Name of the subject identifier column.
rho_grid	A numeric vector of ρ values for the Box-Cox model (default: <code>seq(0.01, 1.2, by = 0.01)</code>).
r_grid	A numeric vector of r values for the log model (default: <code>seq(0.01, 1.2, by = 0.01)</code>).
tau	Optional truncation time. If NULL (default), uses the maximum observed time in the data.
mark_points	Logical; if TRUE (default), marks reference points at $\rho=1$ (open circle, Ghosh-Lin) and $r=1$ (filled circle, proportional odds model).
file	Optional path to save the plot as a PDF (e.g. "loglik_profile.pdf"). If NULL (default), plots to the current device.
width, height	Size of the PDF in inches (default 6 x 4.5); only used when file is given.
verbose	Logical; print progress (default TRUE).
...	Additional arguments passed to wnpml_fit .

Value

A data frame with columns model, param and loglik, invisibly.

Examples

```
bdata <- bladder_prep()
bdata_clean <- bdata[, c("id", "time", "status", "treat", "num", "size")]
plot_loglik(Surv(time, status) ~ treat + num + size,
            data = bdata_clean, id = "id")
```

predict.wnpmle	<i>Predict marginal mean for new covariate values</i>
----------------	---

Description

Evaluates the estimated marginal mean number of recurrent events, $\hat{\mu}(t \mid z) = G\{e^{\hat{\beta}^T z} \hat{\Lambda}(t)\}$, at new covariate values, with pointwise confidence limits.

Usage

```
## S3 method for class 'wnpmle'
predict(
  object,
  newdata = NULL,
  times = NULL,
  conf_int = TRUE,
  conf_level = 0.95,
  ...
)
```

Arguments

object	A wnpmle object.
newdata	A data frame with the same covariates used in fitting (factors may be given as factors or character strings). If NULL, returns the estimated Lambda(t) for the baseline (all covariates = 0).
times	Time points at which to evaluate the marginal mean. If NULL, uses the observed recurrent event times.
conf_int	Logical; if TRUE (default) and standard errors are available, adds pointwise confidence limits.
conf_level	Confidence level (default 0.95).
...	Ignored.

Details

The confidence limits are computed with the delta method from the estimated covariance matrix of (β, Λ) (`vcov(object)`), on the log scale so that they stay positive.

Value

A data frame with column `time` and, for each row `i` of `newdata`, columns `mu_i` and (if `conf_int`) `lower_i` and `upper_i`; or columns `mu` (and `lower`, `upper`) for the baseline.

print.wnpmle	<i>Print method for wnpmle objects</i>
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Description

Print method for wnpmle objects

Usage

```
## S3 method for class 'wnpmle'
print(x, ...)
```

Arguments

<code>x</code>	A wnpmle object.
<code>...</code>	Ignored.

Value

Invisibly returns `x`.

readmission_prep	<i>Prepare the colorectal cancer readmission data for wnpmle analysis</i>
------------------	---

Description

Reads the hospital readmission data of 403 colorectal cancer patients (Gonzalez et al., 2005), shipped with **wnpmle** as a copy of the readmission data from the **frailtypack** package, and converts them to the format used by [wnpmle_fit](#): one row per readmission (status 1) and one final row per patient, which is either death (status 2) or censoring (status 0).

Usage

```
readmission_prep(tau = NULL)
```

Arguments

tau Optional end of follow-up (days). If given, readmissions after tau are removed and patients still under observation at tau (including deaths after tau) are censored at tau. Default NULL: full follow-up.

Details

The data contain 861 rows for 403 patients: 458 readmissions, 109 deaths and 294 censored follow-ups. The Charlson index may change between readmissions; each row carries the value recorded for that interval.

Value

A data frame with columns:

id	Patient identifier.
time	Days since surgery of the readmission, death or censoring.
status	0 = censored, 1 = readmission (recurrent event), 2 = death (terminal event).
chemo	Chemotherapy: factor with levels "NonTreated", "Treated".
sex	Factor with levels "Male", "Female".
dukes	Dukes' tumour stage: factor with levels "A-B", "C", "D".
charlson	Charlson comorbidity index (time-dependent): factor with levels "0", "1-2", "3".

Source

Copy of the readmission data from the **frailtypack** package (Rondeau et al.; GPL (≥ 2)).

References

Gonzalez, J.R., Fernandez, E., Moreno, V., Ribes, J., Peris, M., Navarro, M., Cambray, M. and Borrás, J.M. (2005). Sex differences in hospital readmission among colorectal cancer patients. *Journal of Epidemiology and Community Health*, 59(6), 506-511. doi:[10.1136/jech.2004.028902](https://doi.org/10.1136/jech.2004.028902)

Examples

```
rdata <- readmission_prep()
head(rdata)
table(rdata$status)
table(readmission_prep(tau = 1460)$status)
```

summary.wnpmle	<i>Summary method for wnpmle objects</i>
----------------	--

Description

Summary method for wnpmle objects

Usage

```
## S3 method for class 'wnpmle'
summary(object, tau_grid = TRUE, ...)

## S3 method for class 'summary.wnpmle'
print(x, ...)
```

Arguments

object	A wnpmle object.
tau_grid	Logical; if TRUE (default), also show Lambda at tau/4, tau/2, and tau.
...	Ignored.
x	A summary.wnpmle object.

Value

An object of class summary.wnpmle, printed with the coefficient table and, if tau_grid = TRUE, Lambda at tau/4, tau/2 and tau.

vcov.wnpmle	<i>Extract variance-covariance matrix from a wnpmle object</i>
-------------	--

Description

Returns the full variance-covariance matrix for (beta, Lambda). To get only the beta part, use vcov(fit)[1:p, 1:p].

Usage

```
## S3 method for class 'wnpmle'
vcov(object, ...)
```

Arguments

object	A wnpmle object.
...	Ignored.

Value

A numeric matrix containing the variance-covariance matrix for the regression coefficients and cumulative baseline mean function. Returns an error if `se = "none"` was used in `wnpmle_fit`.

<code>wnpmle_fit</code>	<i>Fit Weighted NPMLE for Survival Data with Recurrent or Competing Events</i>
-------------------------	--

Description

Estimates the weighted nonparametric maximum likelihood estimator (wNPMLE) for the marginal mean function of recurrent events in the presence of a competing terminal event. Two transformation models are supported: the Box-Cox model and the logarithmic model.

Usage

```
wnpmle_fit(
  formula,
  data,
  id = "id",
  type = c("recurrent", "cmprsk", "cmprsk_ltrc"),
  model = c("boxcox", "log"),
  rho = 1,
  tau = NULL,
  se = c("sandwich_adj", "sandwich", "fisher", "none"),
  init_beta = NULL,
  control = list(),
  silent = TRUE
)
```

Arguments

<code>formula</code>	A formula of the form <code>Surv(time, status) ~ covariates</code> , where <code>status</code> takes value 1 for a recurrent event, 2 for the terminal event (e.g. death), and 0 for censoring.
<code>data</code>	A data frame containing the variables in <code>formula</code> and an <code>id</code> column identifying subjects.
<code>id</code>	Name of the subject identifier column in <code>data</code> (default: <code>"id"</code>).
<code>type</code>	Type of analysis. Currently only <code>"recurrent"</code> is supported (recurrent events with a competing terminal event). Future versions will add <code>"cmprsk"</code> (competing risks) and <code>"cmprsk_ltrc"</code> (competing risks with left truncation and right censoring).
<code>model</code>	Transformation model: <code>"boxcox"</code> (default) or <code>"log"</code> .
<code>rho</code>	Transformation parameter. For <code>model = "boxcox"</code> , this is the Box-Cox parameter ρ (default 1, i.e. linear/proportional means model). For <code>model = "log"</code> , this is the parameter r in $G(x) = \log(1 + r \cdot x) / r$ (default 1).

tau	Follow-up truncation time. Kaplan-Meier censoring weights are truncated at tau. If NULL (default), uses the maximum observed time.
se	Variance estimation method: "sandwich_adj" (default, sandwich with censoring correction), "sandwich" (plain sandwich), "fisher" (inverse Hessian), or "none".
init_beta	Initial values for regression coefficients (default: all zeros).
control	A list of control parameters passed to nlminb .
silent	Suppress TMB output (default: TRUE).

Details

Analysis types: Currently only `type = "recurrent"` is implemented, for the recurrent events with competing terminal event setting. Support for `"cmprsk"` (Bellach, Kosorok, Ruschendorf and Fine, 2019) and `"cmprsk_ltrc"` (left truncation and right censoring) will be added in future versions.

Transformation models: The two models differ in the link function G :

- **Box-Cox:** $G(x) = ((1 + x)^\rho - 1)/\rho$, with $G(x) \rightarrow \log(1 + x)$ as $\rho \rightarrow 0$.
- **Logarithmic:** $G(x) = \log(1 + r \cdot x)/r$, with $G(x) \rightarrow x$ as $r \rightarrow 0$.

Both are estimated via automatic differentiation using TMB. The sandwich variance estimator accounts for the estimation of the censoring weights. The censoring-corrected sandwich (`sandwich_adj`) adds an influence function correction for the Kaplan-Meier censoring weight estimation.

Value

An object of class `"wnpml"` with components:

coefficients	Estimated regression coefficients (beta).
se	Standard errors for the regression coefficients.
Lambda	Estimated cumulative baseline mean function, evaluated at the recurrent event times.
lambda	Estimated baseline increments.
event_times	Recurrent event times at which Lambda is estimated.
loglik	Log-likelihood at the optimum.
vcov	Full variance-covariance matrix for (beta, Lambda).
model	Transformation model used.
rho	Transformation parameter used.
tau	Truncation time used.
n	Number of subjects.
n_events	Named vector: recurrent events, terminal events, censored.
convergence	Convergence message from <code>nlminb</code> .
call	The matched call.

References

- Bellach, A. and Kosorok, M.R. (2026). Weighted NPMLE for the marginal mean of recurrent events with a competing terminal event. *arXiv preprint* arXiv:2605.25934. doi:10.48550/arXiv.2605.25934
- Bellach, A., Kosorok, M.R., Ruschendorf, L. and Fine, J.P. (2019). Weighted NPMLE for the subdistribution of a competing risk. *Journal of the American Statistical Association*, 114(525), 259-270. doi:10.1080/01621459.2017.1401540

Examples

```
library(survival)
data("bladder2", package = "survival")
bladder2_prepped <- bladder_prep()

fit <- wnpml_fit(Surv(time, status) ~ treat + num + size,
                 data = bladder2_prepped, id = "id",
                 model = "log", rho = 1)

summary(fit)
```

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